# From Preference Elicitation to Explaining Decisions: a Dialectical Perspective 

Habilitation à Diriger les Recherches Defense

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- My research domain: Artificial Intelligence (Knowledge Representation and Reasoning), Decision Theory;
- Focus of today: our contributions in Multiple Criteria Decision Aiding


## Multiple Criteria Decision Aiding (MCDA)

- At least two actors: an expert, a user;
- set of alternatives/options described (evaluated) on several conflicting point of view/ criteria;

|  | Comfort | Restaurant | Commute time | Cost |
| :---: | :---: | :---: | :---: | :---: |
| $h_{A}$ | $4^{\star}$ | no | 35 min | $120 \$$ |
| $h_{B}$ | $4^{\star}$ | yes | 50 min | $160 \$$ |
| $h_{C}$ | $2^{\star}$ | yes | 20 min | $50 \$$ |
| $h_{D}$ | $2^{\star}$ | no | 30 min | $40 \$$ |

- A decision problem: is option $h_{A}$ better than option $h_{B}$ ? Is option $h_{C}$ good enough? ...
- Sparse preferences between some options;
- Aggregation model containing aggregation procedures


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## An illustrative Example

| Options | Size | Material | Price | Colour | Style |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $a$ | small | Steel | 450 | Red | Classical |
| $b$ | big | Leather | 300 | White | Fashion |
| $c$ | medium | Steel | 320 | Pink | Classical |
| $d$ | small | Leather | 390 | Pink | Sport |

(1) DA: Given your information, $b$ is the best option.
(2) DM: Why is that the case?
(3) DA: Because $b$ is globally better than all other options
(4) DM: What does that mean?
(5) DA: Well... b is top on a majority of criteria considered: the price, the colour, and especially the style, it is so trendy!
(6) DM: But, why $b$ is better than $c$ on the price?
(7) DA: Because $c$ is 20 euros more expensive than $b$.
(8) DM: I agree, but I see that the guarantee is very expensive especially for this watch. In fact I'm not sure to want the guarantee.
(9) DA: But c remains 5 euros more expensive than b.
(10) DM: I see, but this difference is not significant. And also I changed my mind: I would rather to have a classical model, I think it's more convenient for a daily use.
(11) DA: OK. In this case I recommend $c$ as the best choice.
(12) DM: ...

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## MCDA with an Artificial agent !



## Our research issues



## Preference Learning and Elicitation

## Research issues



## Research issues

- Preference modeling issue: how to represent the user's preferences?
- Computational issue: how to build and provide efficient device?

Our Contributions: Mathematical and Computational Tools

## Preference Learning- Overview of our Results



## Overview of our Results-Focus NCS



## NCS: Non-Compensatory Sorting

- an ordered set $C^{1} \prec \cdots \prec C^{p}$ of $p$ predefined categories
- a set of objects to be sorted : $\mathbb{X}=\prod_{i \in \mathcal{N}} \mathbb{X}_{i}$ with $\mathcal{N}=\{1, \ldots, n\}$
- A total preorder, noted $\succsim_{i}$ on $X_{i}, i \in \mathcal{N}$
- approved sets $\left\langle\mathcal{A}_{i}^{k}\right\rangle_{i \in \mathcal{N}, k \in[2 . \text {.p] }}$ defined by a set of limiting profiles $\left\langle b_{i}^{k}\right\rangle_{i \in \mathcal{N}, k \in[2 . . p]}$
- a set of sufficient coalitions $\left\langle\mathcal{T}^{k}\right\rangle_{k \in[2 \text {. .p] }}$ declined per boundary.

$$
\operatorname{NCS}_{\omega}(x)=C^{k} \Leftrightarrow \begin{cases}\left\{i \in \mathcal{N}: x \in \mathcal{A}_{i}^{k}\right\} & \in \mathcal{T}^{k}  \tag{1}\\ \text { and }\left\{i \in \mathcal{N}: x \in \mathcal{A}_{i}^{k+1}\right\} & \notin \mathcal{T}^{k+1}\end{cases}
$$

where $\omega=\left(\left\langle\mathcal{A}_{i}^{k}\right\rangle_{i \in \mathcal{N},}, k \in[2 . . p],\left\langle\mathcal{T}^{k}\right\rangle_{k \in[2 . . p]}\right)$
[Bouyssou and Marchant, 2007a, 2007b]

## NSC - Learning/Disaggregation Step

Inputs: Reference assignments

|  | Cost | Acceleration | Breaking | Road hold | Category |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $m_{1}$ | $16973 €$ | 29.0 sec. | 2.66 | 2.5 | $\star \star$ |
| $m_{2}$ | $18342 €$ | 30.7 sec. | 2.33 | 3 | $\star$ |
| $m_{3}$ | $15335 €$ | 30.2 sec. | 2 | 2.5 | $\star \star$ |
| $m_{4}$ | $18971 €$ | 28.0 sec. | 2.33 | 2 | $\star \star$ |
| $m_{5}$ | $17537 €$ | 28.3 sec. | 2.33 | 2.75 | $\star \star \star$ |
| $m_{6}$ | $15131 €$ | 29.7 sec. | 1.66 | 1.75 | $\star$ |

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## Inputs: Reference assignments

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| :---: | :---: | :---: | :---: | :---: | :---: |
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| $m_{6}$ | $15131 €$ | 29.7 sec. | 1.66 | 1.75 | $\star$ |



| Profile | C | A | B | R |
| :---: | :---: | :---: | :---: | :---: |
| $\star / \star \star$ | $?$ | $?$ | $?$ | $?$ |
| $\star \star / \star \star \star$ | $?$ | $?$ | $?$ | $?$ |

Expected Outputs: Set of sufficient coalitions + Set of profiles

## The Inv-NCS Problem

Finding a solution to an instance of the Inv-NCS problem:

$$
\left(\mathcal{N}, \mathbb{X},\left\langle\succsim_{i}\right\rangle_{i \in \mathcal{N}}, \mathbb{X}^{\star},\left\{C^{1} \prec \ldots \prec C^{p}\right\}, \alpha\right)
$$

where:

- $\mathcal{N}$ is a set of criteria;
- $\mathbb{X}$ is a set of alternatives;
- $\left\langle\succsim_{i}\right\rangle_{i \in \mathcal{N}} \in \mathbb{X}^{2}$ are preferences on criterion $i, i \in \mathcal{N}, \succsim_{i} \subset \mathbb{X}^{2}$ is a total pre-ordering of alternatives according to this criterion;
- $\mathbb{X}^{\star} \subset \mathbb{X}$ is a finite set of reference alternatives;
- $\left\{C^{1} \prec \ldots \prec C^{p}\right\}$ is a finite set of categories totally ordered by exigence level.
- $\alpha: \mathbb{X}^{\star} \rightarrow\left\{C^{1} \prec \ldots \prec C^{p}\right\}$ is an assignment of $\mathbb{X}^{\star}$ to the categories. for a given category $C^{h}, \alpha^{-1}\left(C^{h}\right)=\left\{x \in \mathbb{X}^{\star}: x \in C^{h}\right\}$.


## Inv-NCS - Overview of our Results

Two SAT-based formulations [Belahcène et al., 2018a, 2018c; Tlili et al., 2022]

1. A SAT formulation based on Coalitions

- Explicit representation of the parameter space

2. A SAT formulation based on Pairwise Separation

- Approved sets are given;
- Intuition: for every pair of alternatives ( $g$ accepted, $b$ rejected), is there at least one criterion approving $g$ but not $b$ ?
- Compact SAT formulation; and Inv-NCS is NP-complete
$\leadsto$ The formulations are more efficient than state-of-the art MIP-based approach.


## Inv-NCS - Overview of our Results

MaxSAT relaxations [Tlili et al., 2022]

- Take into account "noisy" data (imperfection in the assessment of performance, mistaken assignment, ...)
- Retrieve the model that restores "the most" examples of the Learning set.


## Preference Learning - The Other contributions

- Majority Sorting Rule (MR-Sort)
- Parameters to learn: limiting profiles $\langle b\rangle$, weights ( $w$ ), threshold ( $\lambda$ );
- Issue: How to deal with an ordered partition $\mathcal{C}=\left(C^{1}, \ldots, C^{h}, \ldots, C^{p}\right)$ that is not monotone w.r.t the natural order of the criterion scale?
- Contribution: taking into account single-peaked preferences - an exact approach and a heuristic approach [Minoungou et al., 2022].
- Ranking with Multiple reference Points (RMP)
- Parameters to learn: weights, reference points, and the lexicographic order on reference points;
- Contribution: A MIP-based approach [Olteanu et al., 2021], a heuristicbased approach [Liu et al., 2014], and a Boolean-based approach [Belahcène et al., 2023a]

XAI \& MCDA

## Our research issues



## Question 2

Given a decision model and a set of preference information, is there a principled way to define simple complete explanations supporting a recommendation/decision?



## Explanation - Issues

- Computation: How difficult is it to produce an explanation?
- Simplicity: Can we keep the explanations simple enough to be processed by a human decision-maker?
- Completeness: Can we explain every 'true' result, that can be deduced from the preference information and the model?
- Soundness: Could we explain 'false' results, claiming the impossibility of an event that could happen or the possibility of an event that cannot happen?


## Explanation - Key Principles [Coste-Marquis and Marquis, 2020; Miller, 2019]

- Explanation shall be rigorous (important decision)
$\rightsquigarrow$ One shall bring proof (complete explanation);
- Explanation shall be understandable
$\rightsquigarrow$ One shall define a language which relates directly to the preferential information (e.g. not include the weights), and be conveyed in an expressive language to the recipient of this explanation.
- Explanation shall be relevant
$\rightsquigarrow$ One shall define what could be pertinent to focus on within the decision situation.
- Explanation shall be simple
$\rightsquigarrow$ One shall define different levels of complexity. We want explanations to be "easy to process" by the recipient of the explanation.


## Explanation in MCDA - Our Contributions



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## Explanation in MCDA - Additive Model

- Preference derives from a value model

$$
\exists V \text { s.t. } x \succsim y \Longleftrightarrow V(x) \geq V(y)
$$

- Value is additive (i.e. $V(x)=\sum_{i} v_{i}\left(x_{i}\right)$ )
- Case: binary evaluation

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ | $g$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s_{1}$ | $\checkmark$ | $x$ | $\checkmark$ | $x$ | $x$ | $x$ | $\checkmark$ |
| $s_{2}$ | $x$ | $\checkmark$ | $x$ | $x$ | $x$ | $\checkmark$ | $\checkmark$ |

$$
\omega=\langle 128,126,77,59,52,41,37\rangle
$$

## Additive Model- Explaining a Pairwise Comparison

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ | $g$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s_{1}$ | $\checkmark$ | $x$ | $\checkmark$ | $x$ | $x$ | $x$ | $\checkmark$ |
| $s_{2}$ | $x$ | $\checkmark$ | $x$ | $x$ | $x$ | $\checkmark$ | $\checkmark$ |

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$$

$$
\left.\begin{array}{l}
\omega\left(s_{1}\right)=128+77+37=242 \\
\omega\left(s_{2}\right)=126+41+37=204
\end{array}\right\} \mathbf{s}_{1} \succ \mathbf{s}_{2}
$$

- Encoding: a vector $\{-1,0,+1\}^{n}$ of arguments in favour (pro) or against (con) or neutral (neu).

$$
\operatorname{pro}_{s_{1}}=\{\boldsymbol{a}, c\}, \operatorname{con}_{s_{1}}=\{\boldsymbol{b}, f\}, \text { while neu }=\{d, e, g\}
$$

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|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ | $g$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $s_{1}$ | $\checkmark$ | $x$ | $\checkmark$ | $x$ | $x$ | $x$ | $\checkmark$ |
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$$

## Question: why $s_{1}$ is preferred to $s_{2}$ ?

## Additive Model- Explaining a Pairwise Comparison

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ | $g$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s_{1}$ | $\checkmark$ | $x$ | $\checkmark$ | $x$ | $x$ | $x$ | $\checkmark$ |
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\operatorname{pro}_{s_{1}}=\{a, c\}, \operatorname{con}_{s_{1}}=\{b, f\}, n e u=\{d, e, \boldsymbol{g}\}
\end{array}
$$

Our proposal -Step-wise Explanations:

$$
s_{1}(a c g) \succ(b f g) s_{2}
$$

## Additive Model- Explaining a Pairwise Comparison

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| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $s_{1}$ | $\checkmark$ | $x$ | $\checkmark$ | $x$ | $x$ | $x$ | $\checkmark$ |
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## Additive Model- Explaining a Pairwise Comparison

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| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
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## Additive Model- Explaining a Pairwise Comparison

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ | $g$ |
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\end{array}
$$

Our proposal-Step-wISE Explanations:

$$
\begin{aligned}
& \mathrm{s}_{1}(a c g) \succ(b c g) \succ(b f g) \mathrm{s}_{2} \\
& \mathrm{~s}_{1}(a c g) \succ(b e f) \succ(b f g) \mathrm{s}_{2} \quad
\end{aligned}
$$

the $1^{\text {st }}$ comparison is complex as it involves 6 criteria.

$$
\begin{gathered}
s_{1}(a c g) \succ(a b c) \succ(b f g) s_{2} x \\
\left(242=\omega_{a}+\omega_{c}+\omega_{g}<\omega_{a}+\omega_{b}+\omega_{c}=331\right)
\end{gathered}
$$

## Additive Model- Explaining a Pairwise Comparison

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ | $g$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s_{1}$ | $\checkmark$ | $x$ | $\checkmark$ | $x$ | $x$ | $x$ | $\checkmark$ |
| $s_{2}$ | $x$ | $\checkmark$ | $x$ | $x$ | $x$ | $\checkmark$ | $\checkmark$ |

$w=\langle 128,126,77,59,52,41,37\rangle$

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\end{array}
$$

Our proposal -Step-wise Explanations:

$$
s_{1}(a c g) \succ(b c g) \succ(b f g) s_{2}
$$

- $\mathrm{S}_{1}(\mathbf{a c g})$ is preferred over $\mathbf{b c g}$, and that $\mathbf{b c g}$ is preferred over (bfg) $\mathrm{S}_{2}$, so that our conclusion should hold, following a transitive reasoning.
- exhibits a collection of statements aiming at proving the decision.


## Additive Model- Explaining a Pairwise Comparison

- Break down the recommendation into "simple" statements;
- the sequence of statements formally support the recommendation.

- Principle-based approach: each scheme is attached to a number of well understood properties of the underlying decision model (e.g. transitivity)
- Cognitively bounded: the statements are constrained to remain "easy" to grasp


## Additive Model- Covering scheme

For the conclusion: $(b f g, c d e)$. The premise $[(f g, c),(b, d e)]$ constitutes a covering scheme:

$$
(f g, c),(b, d e) \xrightarrow{c o v}(b f g, c d e)
$$

Proof diagram

$$
\left.\begin{array}{l}
f g \succ c \xrightarrow{c p} b f g \succ b c \\
\boldsymbol{b} \succ d e \xrightarrow{c p} b c \succ c d e
\end{array}\right\} \xrightarrow{\operatorname{tr}} b f g \succ c d e
$$

Visual representation


Narrative representation
"As, all other things being equal, having free breakfast and wifi access is preferred to having a swimming pool $(\mathbf{f g}, \mathbf{c})$, and being close to the city is preferred than having a sports hall and a low tourist tax (b, de), we get that (bfg, cde)"

## Our Contributions- Argument Schemes for the Additive Model




For a fully specified model:

- \# argument schemes ~\# patterns of reasoning
- \# classes of difficulty of statements
- Complexity results on the existence of an explanation;
- Computing Explanations using ILP;
- Promising experimental results on the explanatory power of the covering scheme.


## Our Explainability Contributions- The Big Picture


[DA2PL, 2018, 2016]

Dialectical Tools

## Our research issues



Given a decision model and a set of preference information, is there a principled way to define simple complete explanations supporting a recommendation/decision?


## Among Challenges

With multiple criteria context, there are many possible decision models. So when deciding whether $a \succ b$ globally, you may use e.g.:

- simple majority ( $\pi_{S M}$ )-count criteria for $a \succ b$ vs. $b \succ a$
- simple weighted majority ( $\pi_{s w m}$ )-same but with weighted criteria
- mean model $\left(\pi_{M}\right)$-sum of utilities of items for each criterion
- weighted sum model ( $\pi_{w s}$ )-same but with weighted criteria
- outranking model-similar to $\pi_{\text {swm }}$ but includes a veto notion
- and many more...


## Among Challenges!

With multiple criteria context, there are many possible decision models. So when deciding whether $a \succ b$ globally, you may use e.g.:

- simple majority ( $\pi_{S M}$ ) -count criteria for $a \succ b$ vs. $b \succ a$
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- and many more...


## Questions:

- is there a principled way to do deal with the multiplicity of models?
- how, in practice, should such interaction be regulated?


## Our contributions - Navigating among Decision Models

- We adopt an axiomatic approach
- Idea: to each model can be attached properties satisfied, e.g.:
- cardinality: the difference of performance is meaningful
- non anonymity: criteria are not exchangeable
- Veto property
- ...
- least specific model is the one that satisfies more properties;



## Our contributions - Argumentation-based Dialogue

- Rely on Multi-Agent Systems tools: interaction protocol, argumentation theory,


Speech acts at each iteration (grey nodes: DM, white nodes: DA).
Key locutions:

- Challenge $(\phi)$-requests some statement that can serve as a basis for justifying or explaining $\phi$.
- $\operatorname{Argue}(\phi, p)-p$ is an explanation of $\phi$.


## How it works? Example

Suppose that a user has to rank four options, e.g. hotels $\{a, b, c, d\}$ evaluated on a set of criteria:
$\left\{c_{1}\right.$ : price, $c_{2}$ : location, $c_{3}$ : stars, $c_{4}$ : breakfast, $c_{5}:$ rating $\}$.

|  | $a$ | $b$ | $c$ | $d$ |
| :--- | :---: | :---: | :---: | :---: |
| price | 80 | 180 | 120 | 60 |
| location | close | far | very far | very close |
| stars | $\star$ | $\star \star \star \star$ | $\star \star \star$ | $\star \star$ |
| breakfast | coffee machine | mini buffet | full buffet | none |
| rating | $120 / 300$ | $3 / 300$ | $267 / 300$ | $278 / 300$ |

Which provides default preferential information:

$$
\begin{array}{ll}
\text { price : } & d \succ_{c_{1}} a \succ_{c_{1}} c \succ_{c_{1}} b ; \\
\text { location: } & d \succ_{c_{2}} a \succ_{c_{2}} a \succ_{c_{2}} c ; \\
\text { stars: } & b \succ_{c_{3}} c \succ_{c_{3}} a \succ_{c_{3}} d ; \\
\text { breakfast: } & c \succ_{c_{4}} b \succ_{c_{4}} a \succ_{c_{4}} d \text {; } \\
\text { rating: } & b \succ_{c_{5}} a \succ_{c_{5}} c \succ_{c_{5}} d .
\end{array}
$$

## How it works? Example



$$
\begin{aligned}
& \mathcal{K B}_{P}^{(1)} \text { contains all statements }\left[x \succ_{c_{i}} y\right] \\
& \mathcal{K B}_{\phi}^{(1)}=\emptyset \\
& \phi_{c}^{(1)}=[b \succ a \succ c \succ d] \\
& \operatorname{miss}\left(\phi_{c}^{(1)}\right)=\phi_{c}^{(1)}
\end{aligned}
$$

## How it works? Example



$$
\begin{aligned}
& \mathcal{K B}_{P}^{(1)} \text { contains all statements }\left[x \succ c_{c_{i}} y\right] \\
& \mathcal{K B}_{\phi}^{(1)}=\emptyset \\
& \phi_{c}^{(1)}=[b \succ a \succ c \succ d] \\
& \operatorname{miss}\left(\phi_{c}^{(1)}\right)=\phi_{c}^{(1)}
\end{aligned}
$$

$$
\mathrm{DA}: \operatorname{Assert}\left(\phi_{1}^{(1)}\right), \phi_{1}^{(1)}=\phi_{c}^{(1)}
$$

## How it works? Example



```
\(\mathcal{K B}_{P}^{(1)}\) contains all statements \(\left[x \succ_{c_{i}} y\right.\) ]
\(\mathcal{K} \mathcal{B}_{\phi}^{(1)}=\emptyset\)
\(\phi_{c}^{(1)}=[b \succ a \succ c \succ d]\)
\(\operatorname{miss}\left(\phi_{c}^{(1)}\right)=\phi_{c}^{(1)}\)
```

DM:Challenge $\left(\phi_{3}^{(1)}\right), \phi_{3}^{(1)}=\{[b \succ a]\}$
Note: $\phi_{3}^{(1)} \subseteq \phi_{c}^{(1)}=[b \succ a \succ c \succ d]$

## How it works? Example



$$
\begin{aligned}
& \mathcal{K B}_{P}^{(1)} \text { contains all statements }\left[x \succ \succ_{c_{i}} y\right] \\
& \mathcal{K B}_{\phi}^{(1)}=\emptyset \\
& \phi_{c}^{(1)}=[b \succ a \succ c \succ d] \\
& \operatorname{miss}\left(\phi_{c}^{(1)}\right)=\phi_{c}^{(1)}
\end{aligned}
$$

DA:Argue $\left(\phi_{5}^{(1)}, p_{5}^{(1)}\right)$,
$\phi_{5}^{(1)}=\{[b \succ a]\}$,
$p_{5}^{(1)}=\left\{\left[b \succ_{c_{3}} a\right],\left[b \succ_{c_{4}} a\right],\left[b \succ_{c_{5}} a\right]\right\}$

## How it works? Example



```
\(\mathcal{K} \mathcal{B}_{P}^{(1)}\) contains all statements \(\left[x \succ c_{i} y\right.\) ]
\(\mathcal{K} \mathcal{B}_{\phi}^{(1)}=\emptyset\)
\(\phi_{c}^{(1)}=[b \succ a \succ c \succ d]\)
\(\operatorname{miss}\left(\phi_{c}^{(1)}\right)=\phi_{c}^{(1)}\)
```

DM:Contradict $\left(\phi_{4}^{(1)}\right), \phi_{4}^{(1)}=\{[a \succ b]\}$

## How it works? Example



$$
\begin{aligned}
& \mathcal{K B}_{P}^{(1)} \text { contains all statements }\left[x \succ \succ_{c_{i}} y\right] \\
& \mathcal{K B}_{\phi}^{(1)}=\emptyset \\
& \phi_{c}^{(1)}=[b \succ a \succ c \succ d] \\
& \operatorname{miss}\left(\phi_{c}^{(1)}\right)=\phi_{c}^{(1)}
\end{aligned}
$$

DA:Challenge $\left(\phi_{6}^{(1)}\right), \phi_{6}^{(1)}=\{[a \succ b]\}$

## How it works? Example



$$
\begin{aligned}
& \mathcal{K B}_{P}^{(1)} \text { contains all statements }\left[x \succ \succ_{c_{i}} y\right] \\
& \mathcal{K B}_{\phi}^{(1)}=\emptyset \\
& \phi_{c}^{(1)}=[b \succ a \succ c \succ d] \\
& \operatorname{miss}\left(\phi_{c}^{(1)}\right)=\phi_{c}^{(1)}
\end{aligned}
$$

$$
\begin{aligned}
& \text { DM:Argue }\left(\phi_{7}^{(1)}, p_{7}^{(1)}\right), \phi_{7}^{(1)}=\{[a \succ b]\} \\
& p_{7}^{(1)}=\left\{\left[a \succ_{c_{1}} b\right],\left[a \succ c_{2} b\right]\right. \\
& \left.\left[c_{1}=\text { strong }\right],\left[c_{2}=\text { strong }\right]\right\}
\end{aligned}
$$

## How it works? Example



$$
\begin{aligned}
& \mathcal{K B}_{P}^{(2)}=\mathcal{K} \mathcal{B}_{P}^{(1)} \cup\left\{\left[c_{1}, c_{2}=\text { strong }\right]\right\} \\
& \mathcal{K B}_{\phi}^{(2)}=\emptyset \\
& \phi_{c}^{(2)}=[d \succ a \succ b \succ c] \\
& \operatorname{miss}\left(\phi_{c}^{(2)}\right)=\phi_{c}^{(2)}
\end{aligned}
$$

Note: $\alpha_{c_{1}}$ and $\alpha_{c_{2}}$ set to 2
$\alpha_{c_{3}}, \alpha_{C_{4}}, \alpha_{c_{5}}$ set to 1
so $d \succ a$
:
:

## Dialectical Vision - Summary

With the idea that preferential information feedback is triggered by the user facing actual recommendations, we formalized:

- a conceptual idea for navigating among models [Labreuche et al., 2015]
- an interaction protocol based on argumentation theory [Labreuche et al., 2015; Ouerdane et al., 2011], where:
- rules and conditions under which we can have a "coherent" interaction in a decision support context, are specified
- Termination can be guaranteed with very few assumptions
- Critics/feedback through Critical Questions (attached to argument schemes).

Summary

## Summary of Our Contributions

- Axe 1- Methods for representing, acquiring and learning preferences
- Formal theory about preferences (representation, learning) and decisions
- Domains: Decision Theory, MCDA, Operational Research;
- Axe 2- Methods for constructing and generating explanations.
- Formal language to communicate the results (recommendations) and "convince" the user.
- Domains: Artificial Intelligence (KRR¹, Argumentation Theory, Logic)
- Axe 3-Methods and tools for structuring and conducing the interaction.
- Formal language to represent the dialogue/interactions and its outcomes;
- Domains: Artificial Intelligence (KRR, MAS², Argumentation theory)

[^0]Perspectives

## Perspectives

Main topic: Explanation-based mixed initiative interaction How to?

- Interleave learning, recommendation and explanation tasks?
- Express and present an explanation?
- Model and manage inconsistency, uncertainty?
- Assess and evaluate the outcomes?
- ...


## Perspectives

## Main topic: Explanation-based mixed initiative interaction

## For what?

- PhD Thesis of Dao Thauvin. Explanatory dialogue for the interpretation of visual scenes. Co-supervision with Stephane Herbin (ONERA) and Céline Hudelot (MICS). - Start 11/2022.
- Keywords: Computer Vision, XAI, Argumentation-based Dialogue



## Perspectives

Main topic: Explanation-based mixed initiative interaction

## For what?

- PhD Thesis Charlotte Calye. Interpretable AI methods for medical research on autoimmune diseases. Supervision, in collaboration with ScientaLab and Céline Hudelot (MICS) - Start 02/2023.
- Keywords: EHR (Electronic Health Records), XAI, Dialog Systems.



## All this was not possible without...

- All my PhD students;
- My co-authors and colleagues;
- Family and friends.


Thank You for your Attention

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[^0]:    ${ }^{1}$ Knowledge Representation and Reasoning
    ${ }^{2}$ Multi-Agent Systems

